

12. Perimeter and Area

- Perimeter of a rectangle = 2 (length + breadth)

Example:

What is the perimeter of a rectangular field whose length and breadth are 15 m and 8 m respectively?

Solution:

Perimeter of rectangular field = $2 (15 \text{ m} + 8 \text{ m}) = (2 \times 23) \text{ m} = 46 \text{ m}$

Perimeter of an equilateral triangle = $3 \times \text{length of a side}$

Perimeter of a square = $4 \times \text{length of a side}$

In general, perimeter of a regular closed polygon = Number of sides of the polygon \times length of each side

Example:

If a farmer wants to fence a square field of length 50 m with 5 rounds of wire then what is the length of the wire required?

Solution:

Length of wire required = $5 \times (\text{perimeter of square field})$

$$= 5 \times (4 \times \text{side})$$

$$= 5 \times [(4 \times 50) \text{ m}]$$

$$= 1000 \text{ m}$$

- Area of a rectangle is given by the formula:

Area of a rectangle = length \times breadth

Example: How much carpet is required to cover a rectangular floor of length 25 m and breadth 18 m?

Solution: Area of the carpet required = Area of rectangular floor

$$= 25 \text{ m} \times 18 \text{ m} = 450 \text{ m}^2$$

- Area of a square is given by the formula:

Area of a square = side \times side

Example: What is the area of a square park of side 10 m 20 cm?

Solution: Length of park = 10 m 20 cm = 10.2 m

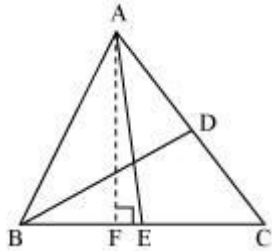
$$\text{Area of park} = 10.2 \text{ m} \times 10.2 \text{ m} = 104.04 \text{ m}^2$$



- Area of a triangle:

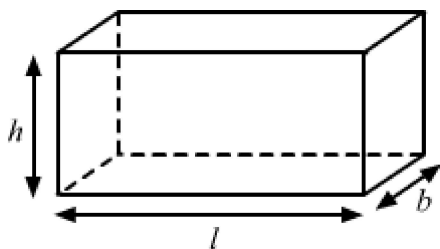
- Area of a triangle = $\frac{1}{2} \times \text{Base} \times \text{Altitude}$
- All the congruent triangles are equal in area, but the triangles having equal areas may or may not be congruent.

Example: $\triangle ABC$ is isosceles with $AC = BC = 6$ cm. AE and BD are the medians and $AF = 4$ cm. What is the area of $\triangle ABD$?



Solution: In $\triangle ABE$ and $\triangle BAD$, we have
 $BE = AD$ $[AC = BC \Rightarrow \frac{1}{2}AC = \frac{1}{2}BC]$
 $\angle ABE = \angle BAD$ $[\text{Angles opposite to equal sides}]$
 $AB = AB$ $[\text{Common}]$
 $\Rightarrow \triangle ABE \cong \triangle BAD$ $[\text{By SAS congruency criterion}]$
 $\text{Area}(\triangle ABE) = \text{Area}(\triangle BAD)$
 Now, $\text{Area} \triangle ABE = \frac{1}{2} \times \text{Base} \times \text{Altitude}$
 $= \frac{1}{2} \times BE \times AF$
 $= \frac{1}{2} \times \left(\frac{6 \text{ cm}}{2}\right) \times 4 \text{ cm}$
 $= 6 \text{ cm}^2$
 $\Rightarrow \text{Area} \triangle ABD = 6 \text{ cm}^2$

- Surface areas of cuboid:



Lateral surface area of the cuboid = $2h(l + b)$

Total surface area of the cuboid = $2(lb + bh + hl)$

Note: Length of the diagonal of a cuboid = $\sqrt{l^2 + b^2 + h^2}$

Example:

Find the edge of a cube whose surface area is 294 m^2 .

Solution:

Let the edge of the given cube be a .

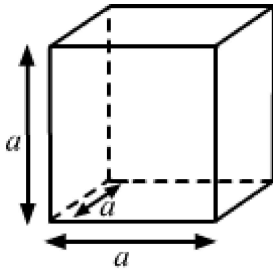
$$\therefore \text{Surface area of the cube} = 6a^2$$

$$\text{Given, } 6a^2 = 294$$

$$\Rightarrow a^2 = 49 \text{ m}^2$$

$$\therefore a = \sqrt{49} \text{ m} = 7 \text{ m}$$

- **Surface areas of cube:**



$$\text{Lateral surface area of the cube} = 4a^2$$

$$\text{Total surface area of the cube} = 6a^2$$

Note: Length of the diagonal of a cube = $\sqrt{a^2 + a^2 + a^2} = \sqrt{3a^2} = \sqrt{3}a$